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OPTIMIZATION OF A LARGE NUMBER OF COOLANT PASSAGES

LOCATED CLOSE TO THE SURFACE OF A TURBINE BLADE

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ABSTRACT

A constrained optimization of locations and discrete radii of a large number of small circular cross-section straight-through coolant flow passages in internally cooled gas turbine vane was developed. The objective of the optimization was minimization of the integrated surface heat flux penetrating the airfoil thus indirectly minimizing the amount of coolant needed for the removal of this heat. Constraints were that the maximum temperature of any point in the vane is less than the maximum specified value and that the distances between any two holes or between any hole and the airfoil surface are greater than the minimum specified value. A configuration with maximum of 30 passages was considered. The presence of external hot gas and internal coolant was approximated by using convection boundary conditions for the heat conduction analysis. A parallel three-dimensional thermoelasticity finite element analysis (FEA) code from the ADVENTURE project at University of Tokyo was used to perform automatic thermal analysis of different vane configurations. A robust semi-stochastic constrained optimizer and a parallel genetic algorithm (PGA) were used to solve this problem using an inexpensive distributed memory parallel computer.

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INTRODUCTION

With a perpetual goal of increasing thermodynamic efficiency of turbines, various vane-cooling schemes have been used. Extensive nozzle vane film cooling that is required for high turbine operating temperatures takes away a significant part of the compressed air flow from the combustor. This leads to a limited amount of the air available for the combustor primary zone, thus reducing "quenching" effect of the air on combustion products and leading to higher NOx levels. As a remedy, a high-pressure closed-circuit internal cooling concept [1] is used that can significantly improve turbine performance. Moreover, circular cross-section straight-through coolant passages became attractive because of the ease of their manufacturing thus lower cost of such vanes. An intuitive approach became to place a large number of such passages very close to the vane outer (hot) surface [2] thus mimicking some of the natural cooling networks appearing in biology. However, the problem that has not been answered yet is where precisely to locate each such coolant passage and what should be the radius of each individual passage.

The design problem considered in this paper involves the parametric shape and topology optimization of coolant passages in a turbine stator vane. We consider configurations that have many small coolant passages that are close to the surface of the vane. All the passage cross-sections are circular. During the design optimization process the radius of each passage may

vary within a specified range, or the passage can be removed completely when its optimized radius reduces below a specified minimum value.

The objective is to reduce the amount of heat transferred through the vane surface subject to a maximum vane temperature. This objective indirectly minimizes the amount of coolant required to maintain an allowable temperature in the vane material. A numerical heat conduction analysis within the vane material is used to compute the objective and the temperature constraint. Instead of a fully three-dimensional conjugate heat transfer analysis [3] or a quasi three-dimensional conjugate heat transfer analysis [4] of each candidate vane configuration, heat convection boundary conditions are used to simulate the presence of coolant and hot gas. This approach includes a very approximate treatment of the fluid mechanics [5] and excludes treatment of elasticity concerns [6]. However, it is sufficient for demonstrating the challenging nature of the design problem and the capabilities of the optimization algorithms used to solve the problem.

The main difficulty in this design problem is due to the large number of design variables and the fact that the design variables for radius are mixed discrete/continuous. Thus, the design variables for passage radius create discontinuities in the objective function space methods based on gradient search. Consequently, methods such as the well-known sequential quadratic programming (SQP) are not appropriate for this problem. Also, the nature of the parameterization of this problem leads to many local minima in the objective function space, which creates difficulties for most optimization algorithms. In this paper we present the results of the application of two global optimization methods that do not require gradients and that are robust against the presence of local minima.

Global search methods will typically require hundreds or thousands of design analyses in attempt to find the global solution [7]. In order to complete the design process in a reasonable amount of time, a parallel computer should be employed. Both the finite element analysis and the optimization codes used in this work were written to make full use of parallel computing resources. The global optimization methods used here are naturally parallel algorithms and can make full use of parallelism.

OPTIMIZATION METHOD REQUIREMENTS

The core of the passage design system is the optimization code. The optimizer directs the design process by generating new designs based on the performance of previous designs, in an iterative manner. In general, we wish to use optimization methods that are robust and efficient. For optimization on a parallel computer, the optimizer should find a good design in the minimum possible number of iterations. Such algorithms should also be capable of making full use of large-scale parallel computers. Since each design analysis is a full 3-D simulation, the total computation time can be from weeks to months if an efficient and sufficiently parallel algorithm is not used.

We also desire a robust optimization algorithm. The optimization process should not terminate in a local minimum and it should not terminate if the analysis cannot be completed occasionally due to, for example, failure to generate a proper grid for a candidate design. For the particular problem considered in this paper, the method should not require gradients of the objective or constraints so that discontinuous design variables can be used (for example, total number of cooling passages which could vary during the optimization).

In our experience, parallel genetic algorithm (PGA) variations [7,8,9,10,] and response surface methods based on Indirect Optimization based on Self Organization (IOSO) [11,12] work well for 3-D turbine coolant passage design optimization.

IOSO Method

The IOSO method is a constrained optimization algorithm based on response surface methods and evolutionary simulation principles. Each iteration of the IOSO method consists of two steps. The first step is creation of an approximation of the objective function(s). Each iteration in this step represents a decomposition of an initial approximation function into a set of simple approximation functions. The final response function is a multilevel graph. The second step is the optimization of this approximation function. This approach allows for self-corrections of the structure and the parameters of the response surface approximation. The distinctive feature of this approach is an extremely low number of trial points to initialize the algorithm (30-50 points for the optimization problems with nearly 100 design variables). The obtained response functions are used in the procedures of multilevel optimization with the adaptive changing of the simulation level within the frameworks of both single and multiple disciplines of the object analysis. During each iteration of the IOSO, the optimization of the response function is carried out within the current search area. This step is followed by the direct call to the mathematical model for the obtained point. The information concerning the behavior of the objective function nearby the extremum is stored, and the response function is made more accurate just for this search area. For a basic parallel IOSO algorithm, the following steps are carried out:

1. Generate a group of designs based on a design of experiments (DOE) method;
2. Evaluate the designs in parallel with the analysis code;
3. Build initial approximation based on the group of evaluated designs;
4. Use stochastic optimization method to find the minimum of the approximation;
5. Do adaptive selection of current extremum search area;
6. Generate a new set of designs in current extremum search area using DOE;
7. Evaluate the new set of designs in parallel with the analysis code;
8. Update the approximation with newly obtained result;
9. Go to 4. unless termination criteria is met.Thus, during each iteration, a series of approximation functions is built for a particular optimization criterion. These functions differ from each other according to both structure and definition range. The subsequent optimization of the given approximation functions allows us to determine a set of vectors of optimized variables, which are used to develop further optimization criteria on a parallel computer.

Multilevel Parallelism in Optimization

The usual approach to parallel optimization is to run a single analysis on each processor per optimization iteration. However, a mesh for a geometrically complex design may be large; sometimes the finite element analysis requires more memory than is available on a single processor. For this reason, the finite element analysis must be distributed among several processors. If a large number of processors are available, we can use all of them by running several simultaneous parallel analyses to evaluate several candidate design configurations. We have developed an optimization communication module with the MPI library [13] that utilizes this multilevel hierarchy of parallelism. This module can be used with any parallel optimization method including PGA and IOSO algorithms. A graphical depiction of the hierarchy of parallelism is shown in Figure 1.
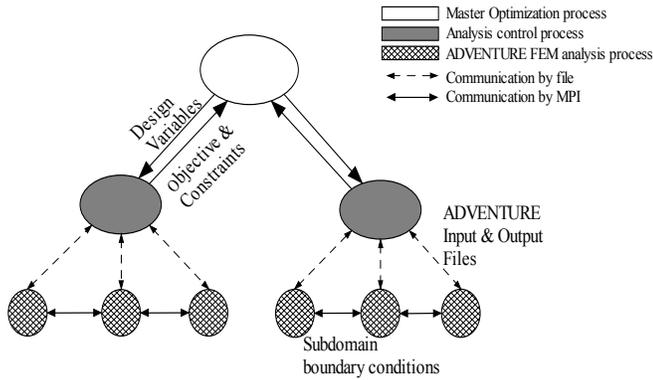

Figure 1: Multilevel parallelism in optimization.

DESIGN ANALYSIS

The thermal analysis was performed by parallel finite element analysis. The finite element analysis codes and tools for mesh generation, mesh partitioning, and others (Fig. 2) are freely available as a part of the ADVENTURE project [14] lead by the University of Tokyo. The finite element solvers are geared towards large-scale parallel analysis and are well suited to the efficient analysis of complicated geometries.
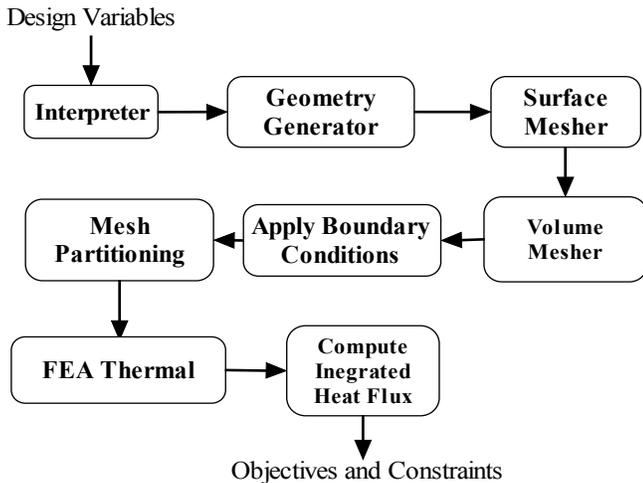

Figure 2: Modules used for automatic parallel FEA.

For each design, a series of modules is required to turn given set of design variables into an object and constraint function values. The flow of data between these modules is depicted graphically in Figure 3. The analysis process may need to be performed hundreds or thousands of times for a single optimization run so it is critical that each module be automatic, robust, and computationally efficient.

OBJECTIVE AND CONSTRAINTS

In this section the design objective and constraint functions are discussed. The objective is to minimize the total amount of heat transferred to the vane (integrated heat flux on the hot surface of the vane) while maintaining a maximum temperature, T_{max}, which is lower than the maximum allowable temperature, T_{allow}. This objective indirectly minimizes the amount of coolant required to cool the vane. The minimization of this objective could result in the reduction of the number of cooling passages as well.

The objective function is computed by integrating heat flux across the vane outer surface, Γ. Mathematically, the objective function F is expressed as

$$F = \int_{\Gamma} k \frac{\partial T}{\partial n} dxdydz \tag{1}$$

where T is the vane temperature, n is the direction normal to the surface Γ, and the constant k is the heat conduction coefficient for the vane material. There are two inequality constraints that are expressed as

$$G_1 = \frac{T_{allow} - T_{max}}{T_{allow}} \tag{2}$$

$$G_2 = \sum_{i=1}^{nholes} C_i \tag{3}$$

where *nholes* is the number of passages and C_i is a positive number when the distance between passage i and another passage is less than a specified distance. Otherwise the value of C_i is zero. The first constraint is necessary so that the maximum temperature in the vane material is always below the maximum allowed temperature. The second constraint is needed to insure that the optimizer only searches for valid geometries. The constraints are satisfied if $G_1 \leq 0.0$ and $G_2 \leq 0.0$.

DESIGN PARAMETERIZATION

The outer vane shape is considered to be fixed and to be provided by the user at the beginning of the design optimization. Presumably, this is the vane shape that has already been optimized for its aerodynamic performance [15]. The design variables include the radius of each circular passage, r_i, and position of the passage center, $<x_i, y_i>$, in the vane cross-section. The passage center is allowed to move normal to the outer contour within a specific region as shown in

Figure 3. The design variable x_i is a distance in the direction normal to the vane surface and is non-dimensionalized so that it always lies between the two dashed lines shown in Figure 4. The variable y_i is a non-dimensional distance in a surface following coordinate direction that is taken along the outer surface of the vane. The variable y_i is measured from the leading edge in the clockwise direction. For 30 passages, this parameterization leads to a total 90 variables.
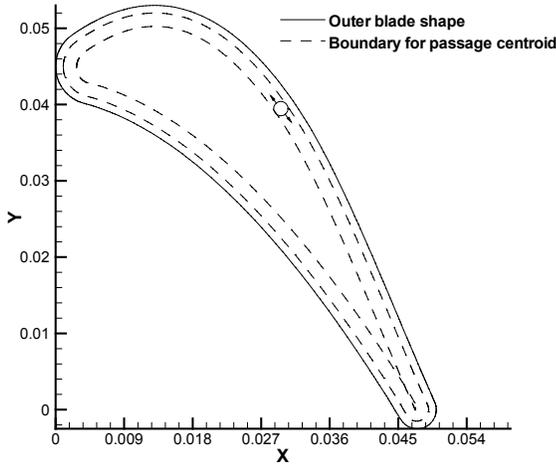

Figure 3. Region where coolant passage centers are allowed.

A triangular surface mesh [16] and a tetrahedral volume mesh [17] were generated automatically for each candidate design. The mesh generator did an adequate job of placing enough points between the passages and the vane surface, even when the passages were very close to the surface. Example meshes are shown in Figures 4 and 5. A typical mesh had around 80,000 nodes.
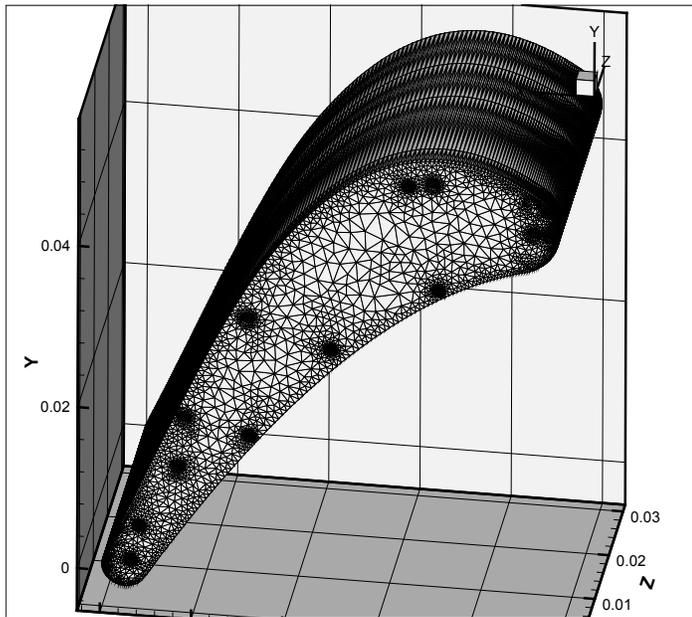
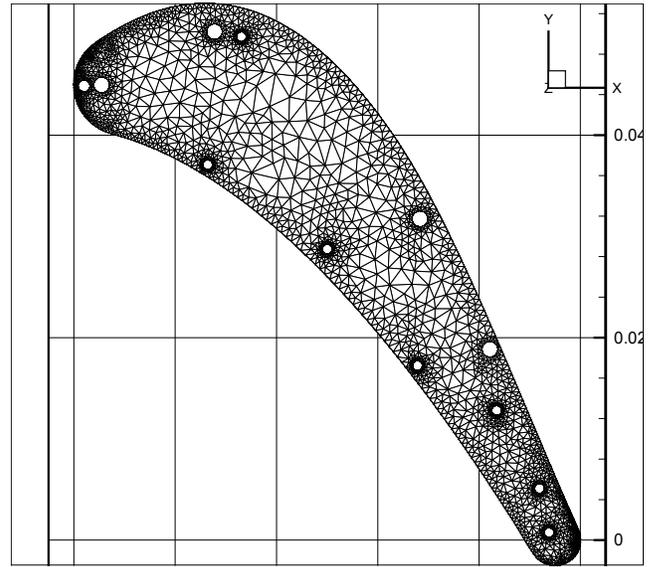

Figure 4: View of a surface mesh.

Figure 5: View of mesh on a vane cross-section.

DESIGN OPTIMIZATION EXAMPLE
In this section, an example of design optimization using both GA and IOSO optimization methods are presented. For all cases the design variable bounds were set according to Table 1. Additional constants used for the example are shown in Table 2. The initial passage distribution was determined by the functions given for the suction and pressure sides, respectively, as

$$y_i = y_{te}(0.5451567\,tanh(\frac{\pi}{16}(i-1)-\frac{\pi}{2})+0.5) \qquad (4)$$

$$y_i = (1-y_{te})(0.5451567\,tanh(\frac{\pi}{14}(i-17)-\frac{\pi}{2})+0.5)+y_{te} \qquad (5)$$

where y_{te} is the y location of the trailing edge. These functions provide a clustering of the passages near the leading and trailing edges.

Table 1: Design variable bounds

Parameter	Lower bound	Upper bound
r_i	0.5 mm	0.8 mm
x_i	1.0 mm	1.525 mm
y_i	$\dfrac{y_{i-1}+y_i}{2}$	$\dfrac{y_i+y_{i+1}}{2}$

Table 2: Constants used for design examples

Maximum allowable temperature, T_{allow}	900.0 ^{o}C
Vane heat conduction coefficient, k	9.0 W/m-^{o}C
Vane span, L	5.0 cm
Vane axial chord length	5.0 cm
Minimum allowable distance between passages	0.1 mm

The outer vane geometry was generated by creating a series of 2-D turbine airfoils [10] and stacking the sections along the vane spanwise direction. Though the generated geometry is not an actual stator vane, we tried to make an outer surface that maintains the characteristic shape of a typical turbine stator. However, if a real outer shape is available from the user, it should be possible to use it directly with the design system with no modifications.

Thermally insulated conditions were used on the vane end surfaces. Convective heat transfer (Robin type) boundary conditions were used on the surfaces of the coolant passages and on the outer vane surface. The coolant was assumed to be water vapor with the parameters given in Table 3. The values for bulk coolant temperature and coolant convective heat transfer coefficients were approximated by a simplified analysis.

Table 3: Constants used for finding T_c and h_c for the coolant

Inlet temperature, T_{inlet}	25.0 °C
Reynolds number, Re	6.0×10^4
Prandtl number, Pr	6.12
Inlet velocity, U_{inlet}	30.0 m/s
Assumed average wall temperature, T_{wall}	662.5 °C
Passage diameter, d	1.8 mm

An approximation for the Nusselt number, Nu, for flow through a cylinder is given by the following equation.

$$Nu = 0.023\, Re^{0.8}\, Pr^{0.4} \qquad (6)$$

The convective heat transfer coefficient, h_C, can be found from the definition of the Nusselt number.

$$h_c = \frac{k_c Nu}{d} \qquad (7)$$

The coolant exit temperature, T_{exit}, can be found by the equation below.

$$T_{exit} = T_{wall} - (T_{wall} - T_{inlet})e^{-\frac{h_c \pi d L}{\dot{m} Cp}} \qquad (8)$$

Once the exit temperate is known, the approximate bulk coolant temperature is given as a function of vane span in the z direction.

$$T_c = T_{inlet} - (T_{inlet} - T_{exit})\sqrt{\frac{z}{L}} \qquad (9)$$

Table 4 shows the exact values used for the convection boundary conditions for this example.

An example design optimization was performed. The maximum number of coolant passages was set to 30. The total number of design variables was 90. This problem was solved using both PGA and IOSO algorithms. For both PGA and IOSO method, 40 simultaneous analyses were run per iteration.

Each finite element heat conduction analysis used 2 processors. The same initial design was given to both optimizers at the start of each run. The following PGA parameters were used: 5.0 percent mutation rate, 50.0 percent chance of uniform crossover, 7 bit binary encoding for y_i and 5 bit encoding for x_i, r_i.

Table 4: Parameters for initially 30-passage optimization.

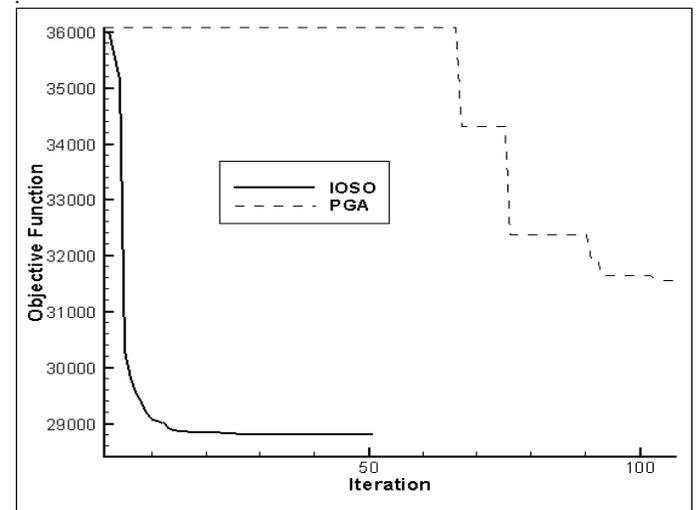|	
Coolant bulk temperature, T_C	$\left(25.0 + 57.9\left(\frac{z}{L}\right)^{1/2}\right)$ °C
Coolant convection heat transfer coefficient, h_C	107400.0 W/m²-°C
Hot gas bulk temperature, T_B	$\left(1350.0 - 150.0\frac{x}{c}\right)$ °C
Hot gas convection heat transfer coefficient, h_B	$h_B = 5300.0 + 1100000.0\left[\frac{x}{c} - 0.53\right]^4$ W/m²-°C

Figure 6: Objective function convergence history.

The convergence history in Figure 6 shows that for this example the IOSO method outperforms the PGA method. Both IOSO and PGA methods reduced the total heat flux from the initial design as shown in Table 5. However, one can see in Figure 10 that the topology of the passages is slightly different between the two best designs. The result of the PGA is clearly a local optimum since some passages are clustered to closely together near the leading and trailing edge creating overcooled areas. The passage size and position for the IOSO result is more uniform than the PGA result. More iteration and more fine-tuning of control parameters, including increasing the selection pressure, could further improve the PGA result.

The outer surface temperature on the optimized design is much closer to T_{allow} than in the initial design as shown in Figure 7. The best possible design could be achieved if the entire outer surface temperature would be equal to T_{allow}. In that case, the smallest possible integrated heat flux would be 19830.0 Watts. However, a perfect design is not achievable due to the limitations of the geometric parameterization.
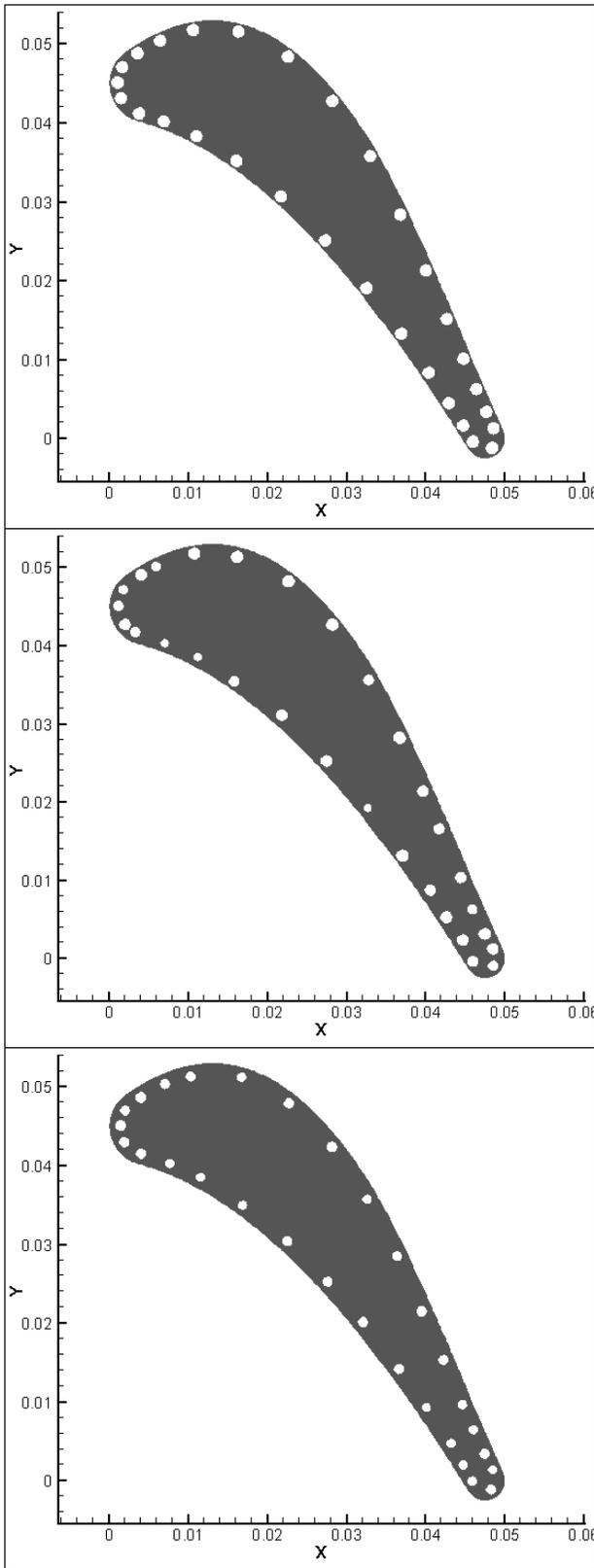
Figure 7: Cooling passages for initial design (top),
PGA best design (middle), and IOSO best design (bottom)
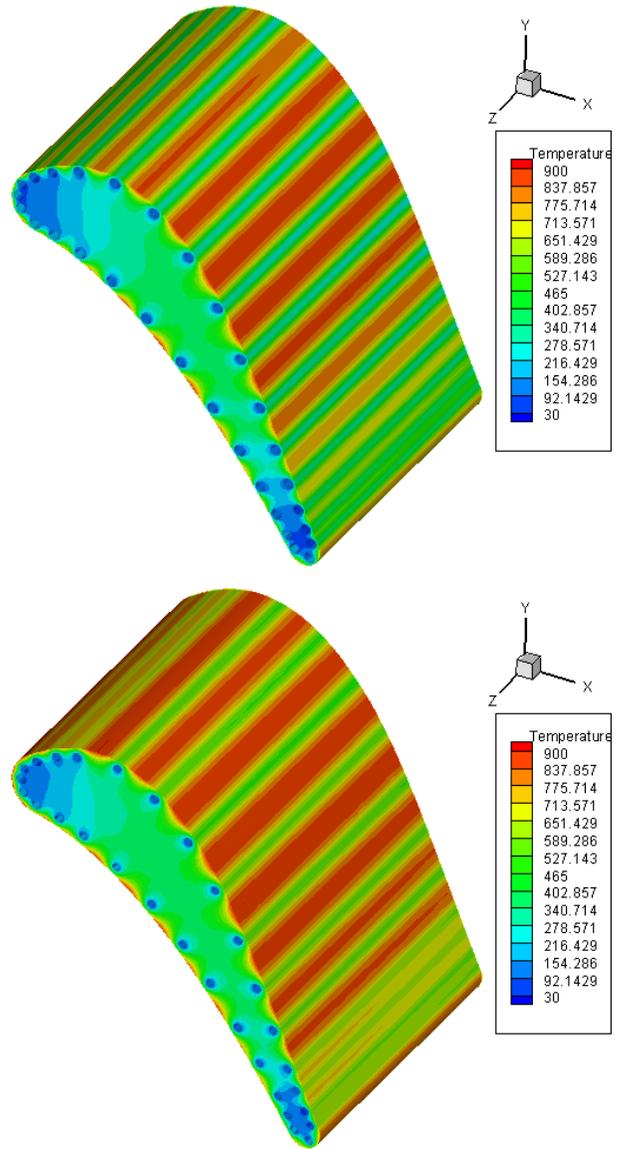for initially 30-passage case.

Figure 8: Temperature distribution on suction side for initial
design (top) and IOSO optimized best design (bottom).

Table 5: Optimization results.

Result	Initial guess	PGA best design	IOSO best design
nholes	30	30	30
T_{max}	892.6 ^{o}C	899.1 ^{o}C	902.3 ^{o}C
F	36099.8 W	31563.0 W	28808.2 W

CONCLUSIONS

A software system for the design of turbine vane coolant
passages has been developed using powerful optimization
algorithms and efficient parallel finite element thermal field
analysis code. The automatic parametric shape design of many
internal coolant passages was demonstrated. A typical design
optimization can be completed within a few hours using an
inexpensive cluster of personal computers. The IOSO

optimization method was found to produce better results with fewer iterations than the PGA method. The IOSO method is also more robust and easier to use since it requires fewer tuning parameters than the PGA method.

The design optimization examples presented in this paper represent simplified cases as the effect of the inner and outer fluid mechanics is very approximate. The next step towards a complete automatic design system should be to add 3-D fluid mechanics analysis codes and 3-D thermoelasticity analysis thus providing a fully 3-D conjugate analysis environment. However, this would then increase computing time by an order of magnitude. But, with the recent availability of low cost parallel supercomputing based on commodity component, a complete multidisciplinary design system may be proven to be computationally and financially feasible in the very near future.

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